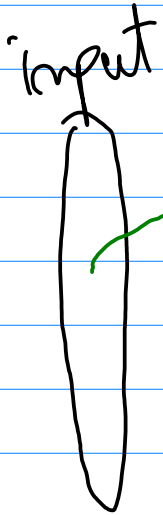


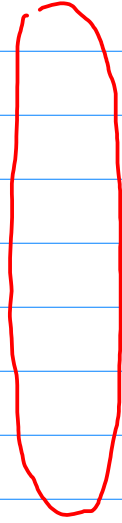
# Course 4

## Neural network

Layer 1    Layer 2 ...



values in  $\mathbb{R}^N$



Output

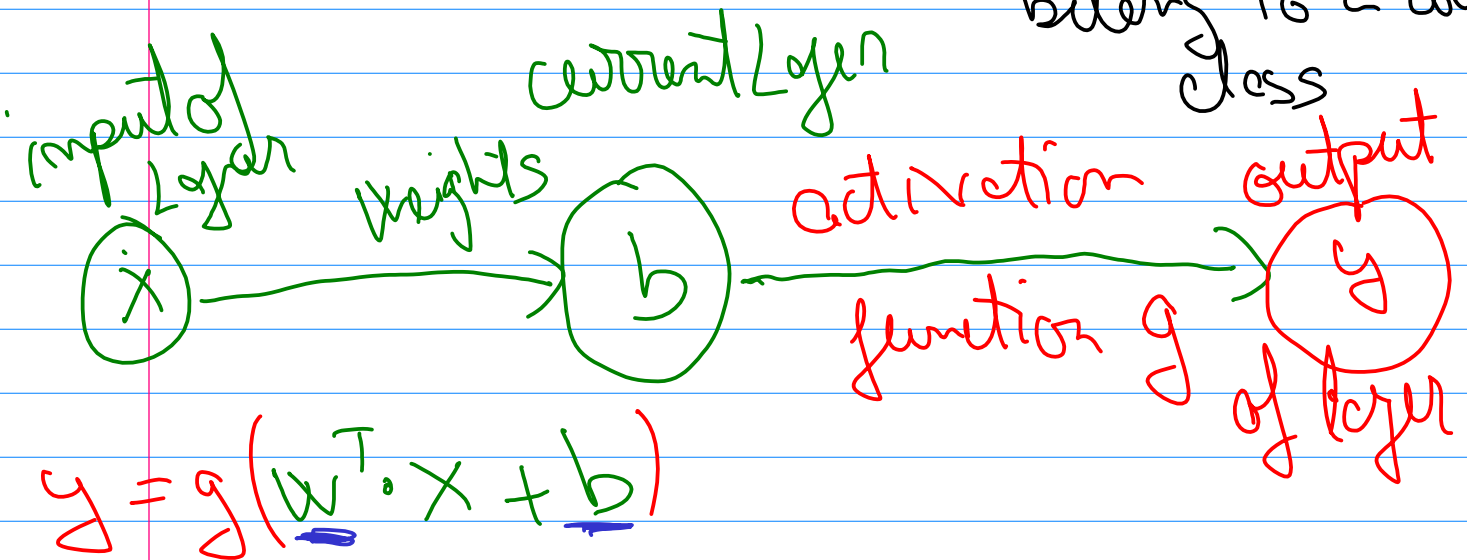


tensor: scalar  
vector etc

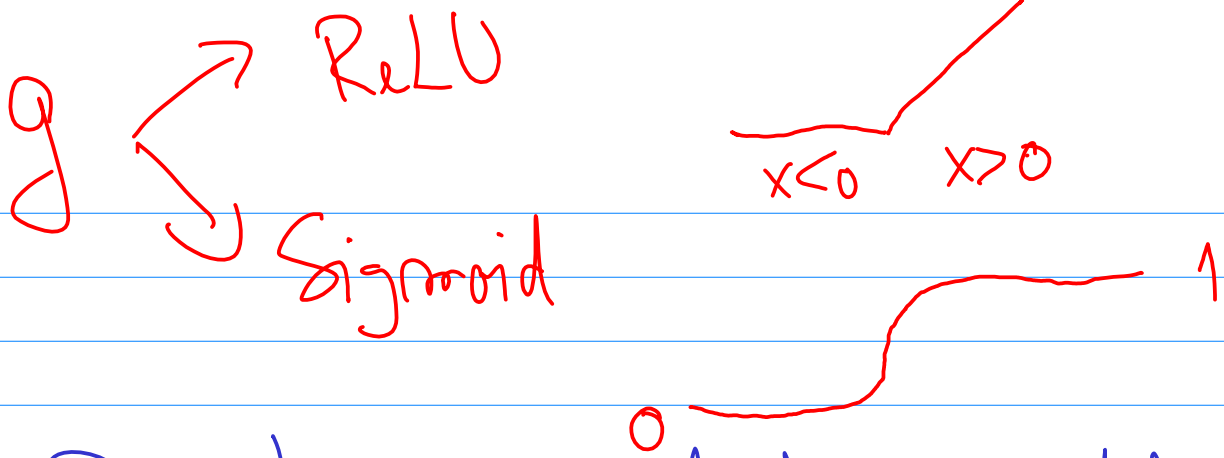
any "tensor"

Scalar, vector, matrix  
3D matrix etc.

Classification pb  
probability to  
belong to a certain  
class



$$y = g(\underline{w}^T \cdot x + \underline{b})$$



→ Deep Learning: find parameters of a given neural network such that it behaves "like we want"

→ We need Data:

Structure

input<sub>1</sub>

output<sub>1</sub>

⋮

input<sub>N</sub>

output<sub>N</sub>

→ Split data into train set (80%) and test set (20%)

Testing: checking results of the model on things it hasn't seen before.

→ Learning:

→ Loss function:

Examples:

$$\sum_k | \text{model}(\text{input}_k) - \text{output}_k |$$

depends on  $W, b$

close

→ The structure of the network is fixed before training.

→ Learning: optimization algorithm minimize the loss function

→ Non-linear activation functions are needed in order to capture "interesting" (non linear) phenomena

1. A simple example: learning a 1D function. Using a network on data which is very different than the training data will not provide useful results.

Exercise: learn a 1D function on  $[-1, 1]$  and test it for values in a larger interval.

Neural networks  $\rightarrow$  universal function approximators

$f(x) = x^2$

$\rightarrow$  Data      Input  $x_i \rightarrow$  Output  $x_i^2$  | split into train/testing

$\rightarrow$  define a model (Network)

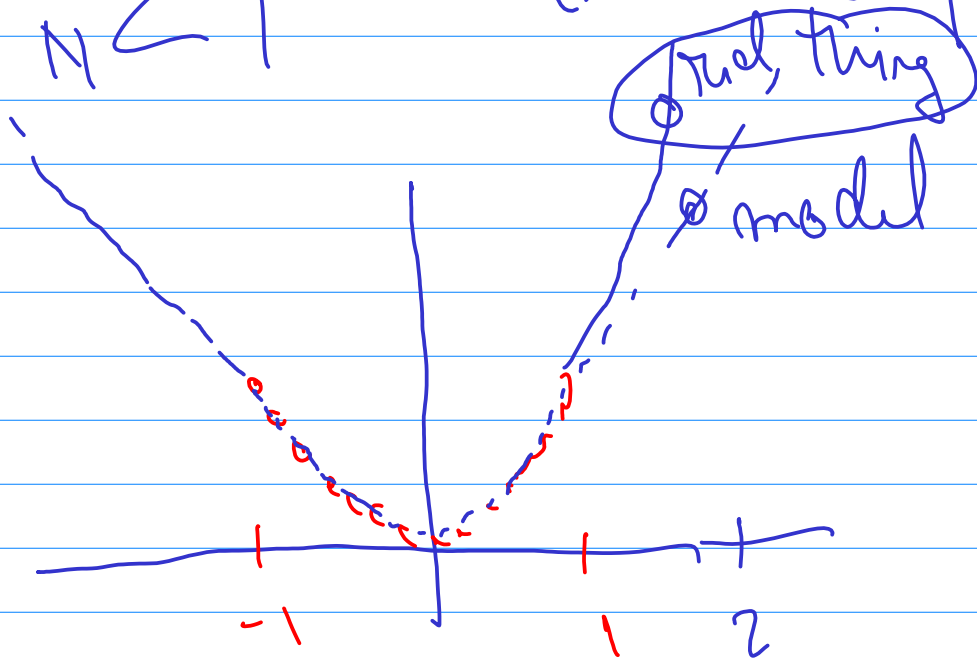
$\rightarrow$  Training

$\rightarrow$  Testing

Dim input = 1  
Dim output = 1

Mean Square Error Loss

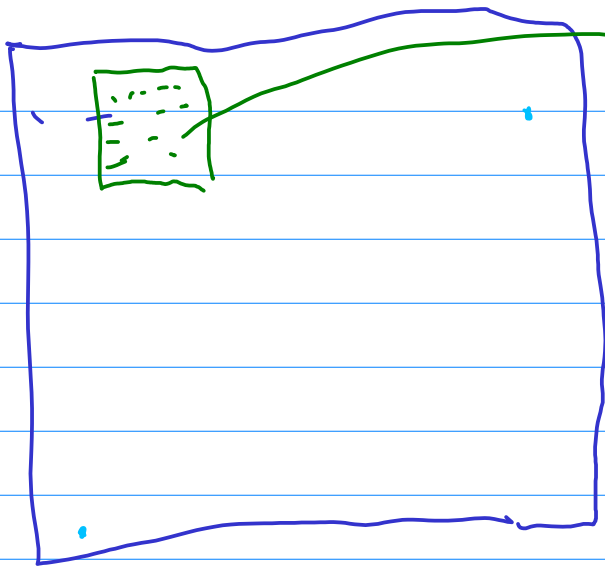
$$\frac{1}{N} \sum | \text{model}(x_i) - \text{output}_i |^2$$



Images are not just values



We need to interpret together pixels that are close geometrically.



→ aggregate pixels  
using a moving frame